Performance Evaluation of Machine Learning Systems

R. Basili, S. Filice

University of Roma Tor Vergata

Web Mining e Retrieval 2022/2023

Motivations

- Is a ML system performing properly?
- Among a set of different algorithms/models, which one is performing better on a given task?
- What can I do to improve my target classification system?

Overview

- Performance Evaluation Metrics
  - Classifier Evaluation Metrics
  - Information Retrieval Systems Evaluation Metrics
- Tuning and Evaluation Methods
- Error Diagnostics

Classifier Evaluation: Confusion Matrix

		PREDICTED VALUE		
		Class A	Class B	Class C
ACTUAL VALUE	Class A	38	12	0
	Class B	5	43	2
	Class C	6	0	44

$$accuracy = \frac{\#correct\ classifications}{\#classifications} = \frac{38 + 43 + 44}{150} = 83.33\%$$

$$error\ rate = \frac{\#incorrect\ classifications}{\#classifications} = \frac{12 + 5 + 2 + 6}{150} = 16.67\%$$

Evaluation with skewed data

- Accuracy is not a suitable metric for task with imbalanced classes (for instance a spam detector)

		PREDICTED VALUE	
		Spam	Non-Spam
ACTUAL VALUE	Spam	0	10
	Non-Spam	0	9990

Very bad performance on the Spam class, that is the target of the classifier!!

… nonetheless …

$$accuracy = \frac{\#correct\ classifications}{\#classifications} = \frac{9990}{10000} = 99.9\%$$

Single Class Metrics

		PREDICTED VALUE	
ACTUAL VALUE		Class C	Not Class C
	Class C	**TP** True Positive	**FN** False Negative
	Not Class C	**FP** False Positive	**TN** True Negative

$$precision = \frac{TP}{TP + FP}$$

what percentage of instances the classifier labeled as positive are actually positive?

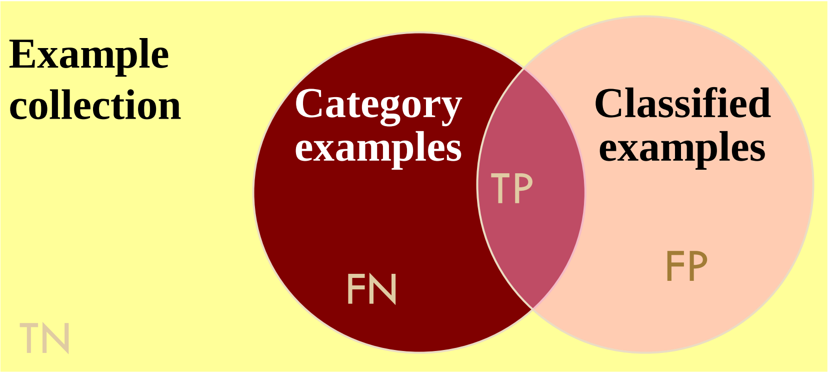
$$recall = \frac{TP}{TP + FN}$$

what percentage of positive instances did the classifier label as positive?

$$F1 = \frac{2 \times precision \times recall}{precision + recall}$$

F-measure is the harmonic mean of precision and recall

Class-based evaluation



	Classified	Rejected
Not Members	Classified but not Members	Rejected & not Members
Members	Classified & Members	Rejected but Members

$$precision = \frac{\#\ of\ Members\ Classified}{\#\ of\ Members\ Classified\ + \#\ of\ Classified\ not\ Members}$$

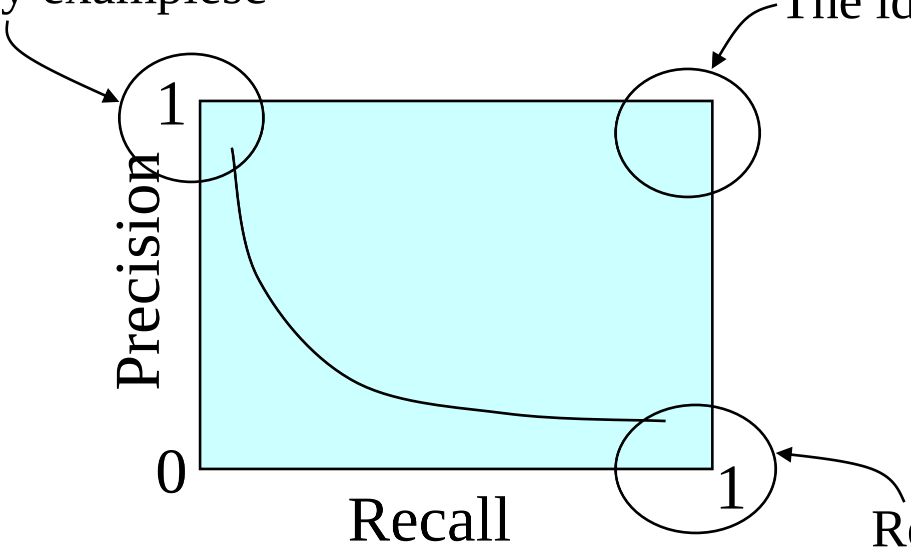
$$recall = \frac{\#\ of\ Members\ Classified}{\#\ of\ Members\ Classified\ + \#\ of\ Rejected\ Members}$$

What about accuracy???

Trade-off between Precision and Recall

Classify members but still misses many examplesc

The ideal

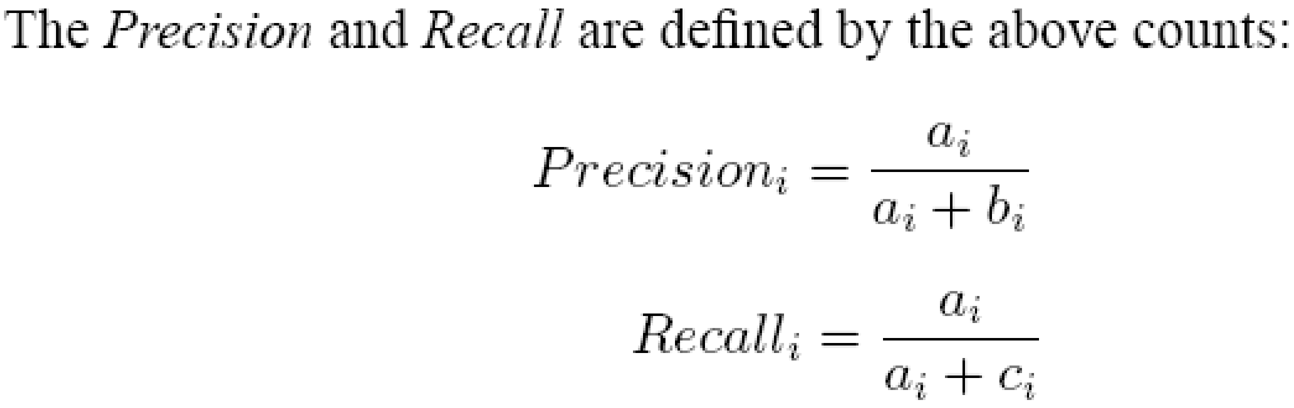


Returns most members but also lots not members

Other class based measures

Precision and Recall of C_i

- a, corrects (TP_i)
- b, mistakes (FP_i)
- c, instances of a $Class_i$ that are not actually retrieved, (FN_i)



The *Precision* and *Recall* are defined by the above counts:

$$Precision_i = \frac{a_i}{a_i + b_i}$$

$$Recall_i = \frac{a_i}{a_i + c_i}$$

		PREDICTED VALUE		
		Class A	Class B	Class C
ACTUAL VALUE	Class A	38	12	0
	Class B	5	43	2
	Class C	6	0	44

- □ $\text{Precision}_A = 38/(38+5+6)=38/49$
- □ $\text{Recall}_A = 38/(38+12)=38/50$

- □ $\text{Precision}_B = 43/(43+12)=43/55$
- □ $\text{Recall}_C = 44/(44+6)=44/50$

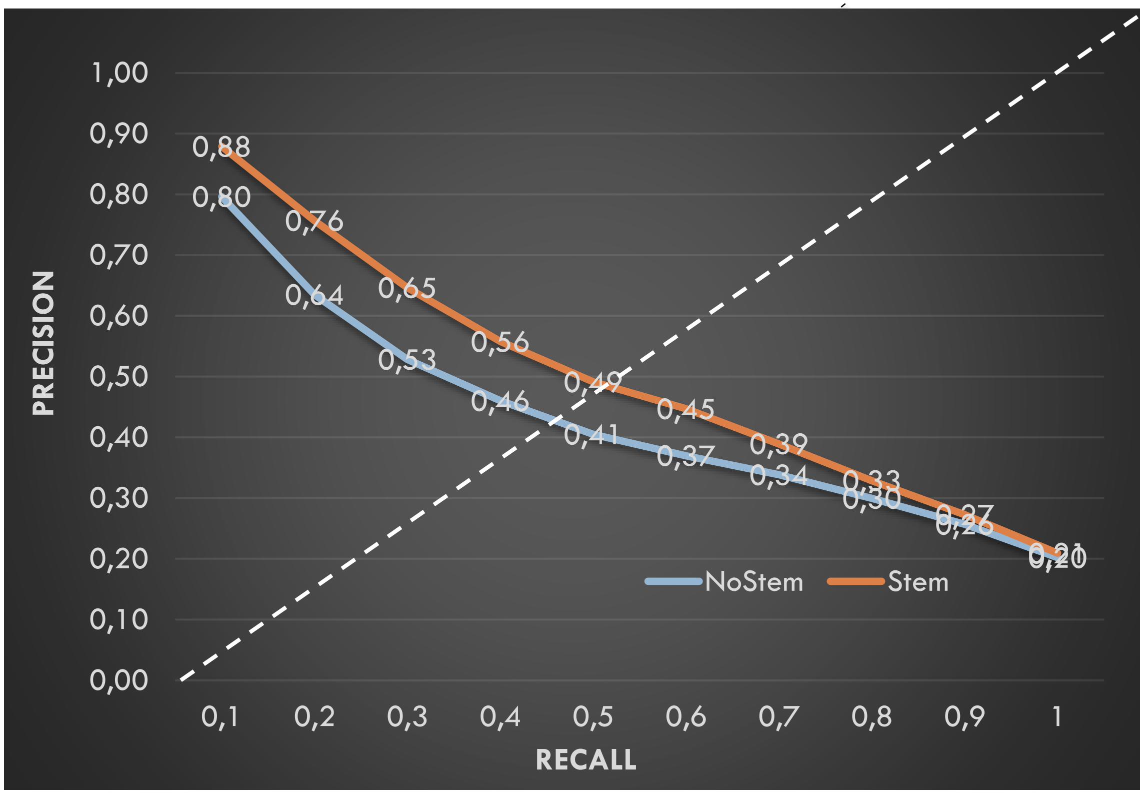
Performance Measurements (cont’d)

- Breakeven Point
  - Find thresholds for which

    Recall = Precision
  - Interpolation
- F-measure $F_1 = \frac{2 \times Precision \times Recall}{Precision + Recall}$
  - Harmonic mean between precision and recall
- Global performance on more than two categories
  - Micro-average
    - The counts refer to classifiers
  - Macro-average (average measures over all categories)

Break-even Point

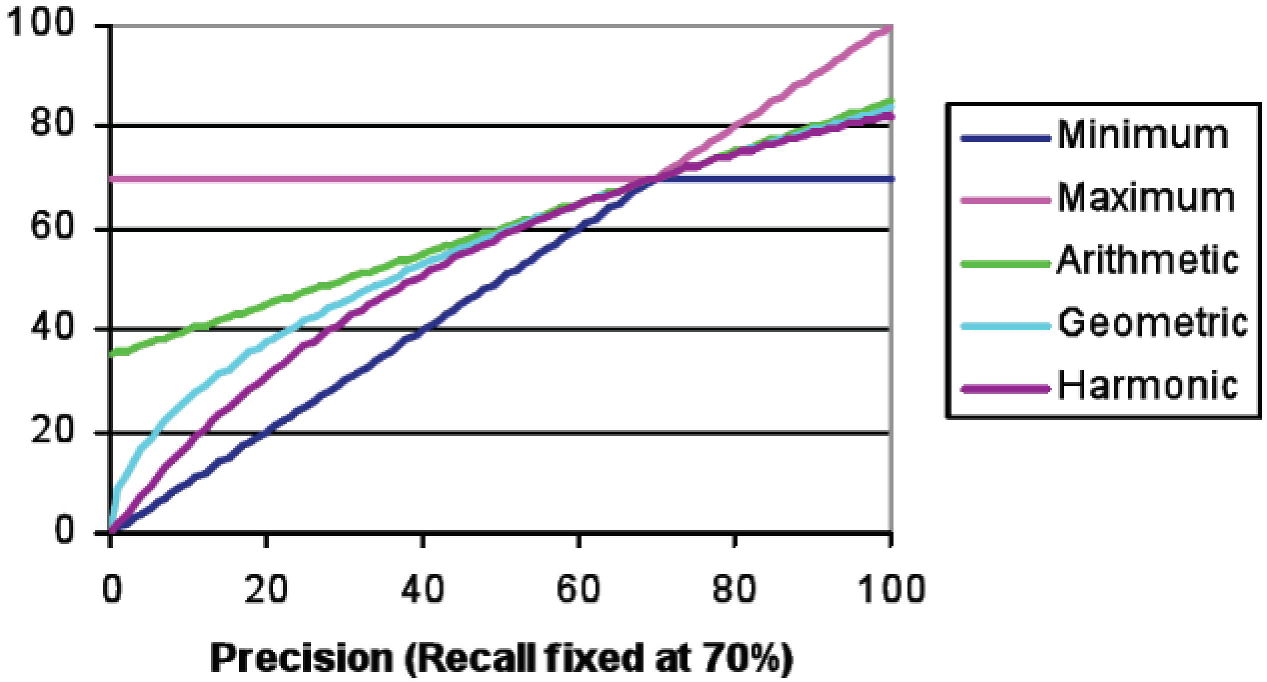
- The BEP is the interpolated estimate of the value for which Recall=Precision



- It shows the superiority of methods whose behavior is closer to the (1,1) ideal performance

Averaging Precision & Recall:
A comparison

$$F_1 = \frac{2}{\frac{1}{Precision} + \frac{1}{Recall}} = \frac{2 \cdot Precision \cdot Recall}{Precision + Recall}$$



$$\min(p, r)$$
$$\max(p, r)$$

$$arithM(p, r) = \frac{p + r}{2}$$

$$geomM(p, r) = \sqrt{p \cdot r}$$

$$harmM(p, r) = \frac{2}{p^{-1} + r^{-1}}$$

Averaging Precision & Recall: cross-categorical analysis

- Individual scores characterize the performance about each specific class
- Simple macro averaging can be applied to have

$$MPrecision = \sum_{i=1}^{n} Precision_i$$

$$MRecall \quad = \sum_{i=1}^{n} Recall_i$$

$$MF_1 \quad = \frac{2 \cdot MPrecision \cdot MRecall}{MPrecision + MRecall}$$

F-measure e MicroAverages

$$F_1 = \frac{2 \times Precision \times Recall}{Precision + Recall}$$

$$\mu Precision = \frac{\sum_{i=1}^{n} a_i}{\sum_{i=1}^{n} a_i + b_i}$$

$$\mu Recall = \frac{\sum_{i=1}^{n} a_i}{\sum_{i=1}^{n} a_i + c_i}$$

$$\mu BEP = \frac{\mu Precision + \mu Recall}{2}$$

$$\mu f_1 = \frac{2 \times \mu Precision \times \mu Recall}{\mu Precision + \mu Recall}$$

		PREDICTED VALUE		
		Class A	Class B	Class C
ACTUAL VALUE	Class A	38	12	0
	Class B	5	43	2
	Class C	6	0	44

- $\text{Precision}_A = 38/(38+5+6)=38/49$
- $\text{Precision}_B = 43/(43+12)=43/55$
- Segue che:

$$\text{Mprecision}=1/3(38/49 + 43/55 +\ldots)$$

		PREDICTED VALUE		
		Class A	Class B	Class C
ACTUAL VALUE	Class A	38	12	0
	Class B	5	43	2
	Class C	6	0	44

- $\text{Precision}_A = 38/(38+5+6)=38/49$
- $\text{Precision}_B = 43/(43+12)=43/55$
- Segue che:

  $\mu\text{Precision}=(38+43+44)/(38+43+44+11+12+2)$

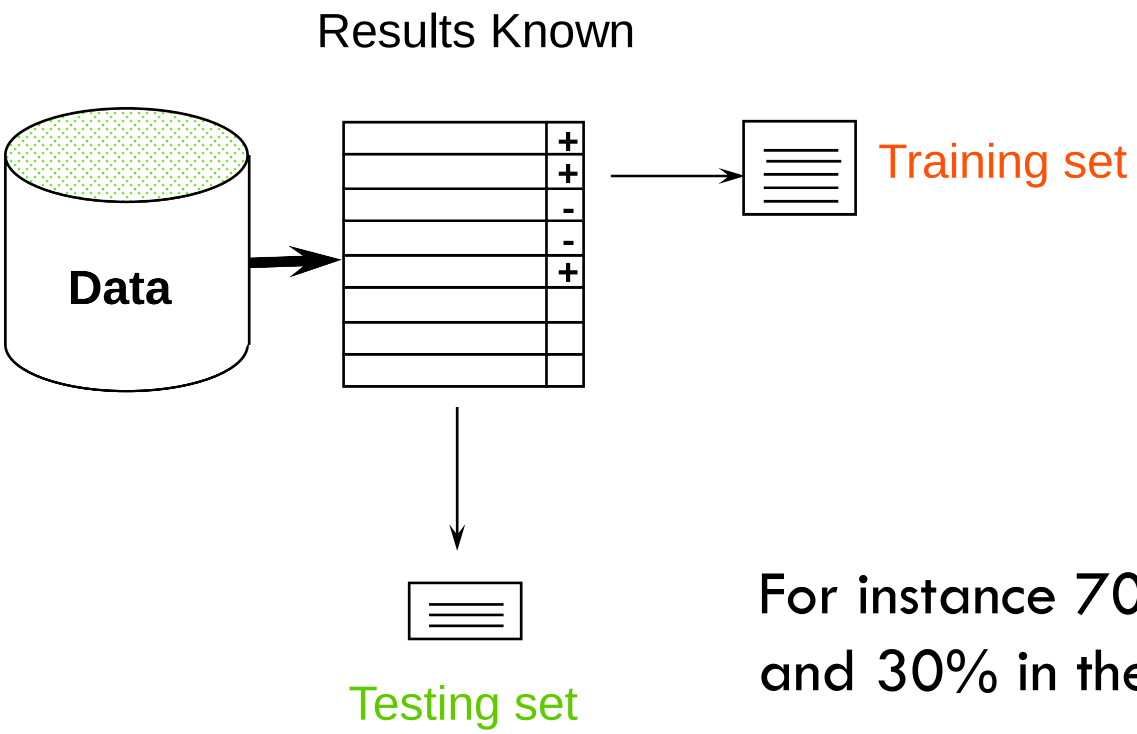
Overview

- Performance Evaluation Metrics
  - Classifier Evaluation Metrics
  - Information Retrieval Systems Evaluation Metrics
- **Tuning and Evaluation Methods**
- Error Diagnostics

Testing Data

- To obtain a reliable estimation, test data **must be** instances **not** employed for the training step:
  - Error on the training data is *not* a good indicator of performance on future data, because new data will probably not be **exactly** the same as the training data!
  - *Overfitting* – fitting the training data too precisely - usually leads to poor results on new data
  - We want to evaluate how much accurate predictions of the model we learned are, and not other computational aspects (e.g. its memorization capability)

Step 1: dataset splitting



Results Known

Data

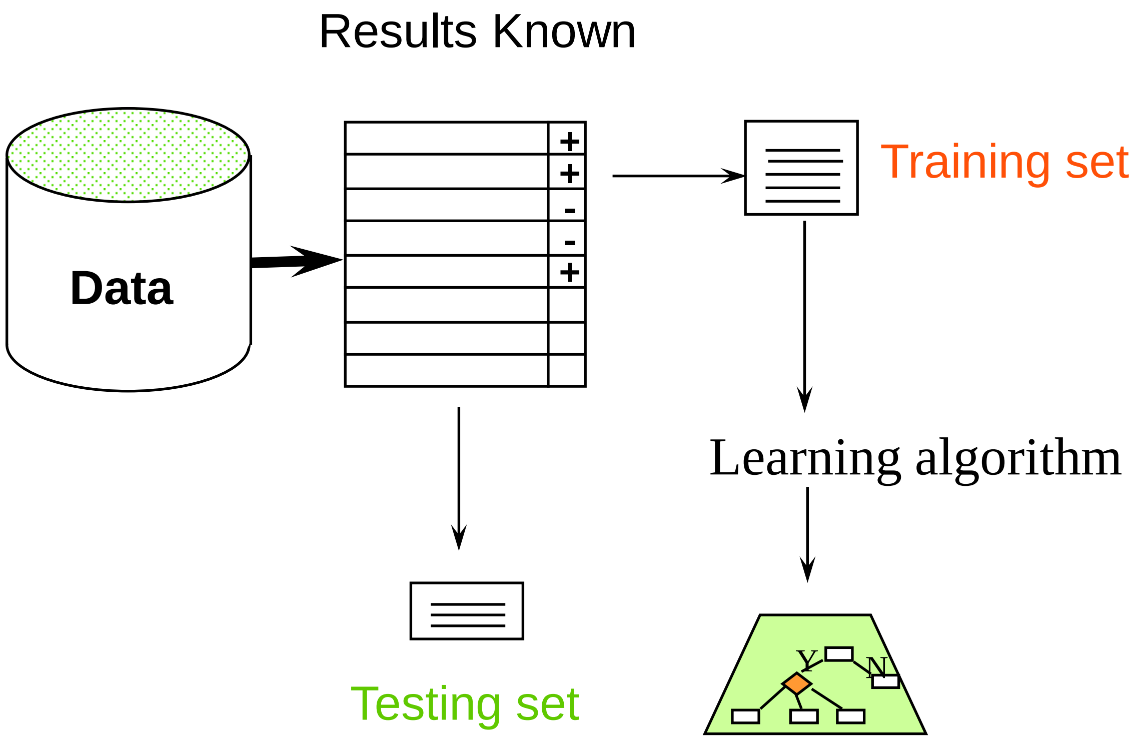
+
+
-
-
+

Training set

Testing set

For instance 70% in the training set and 30% in the test set

Step 2: learning phase



Results Known

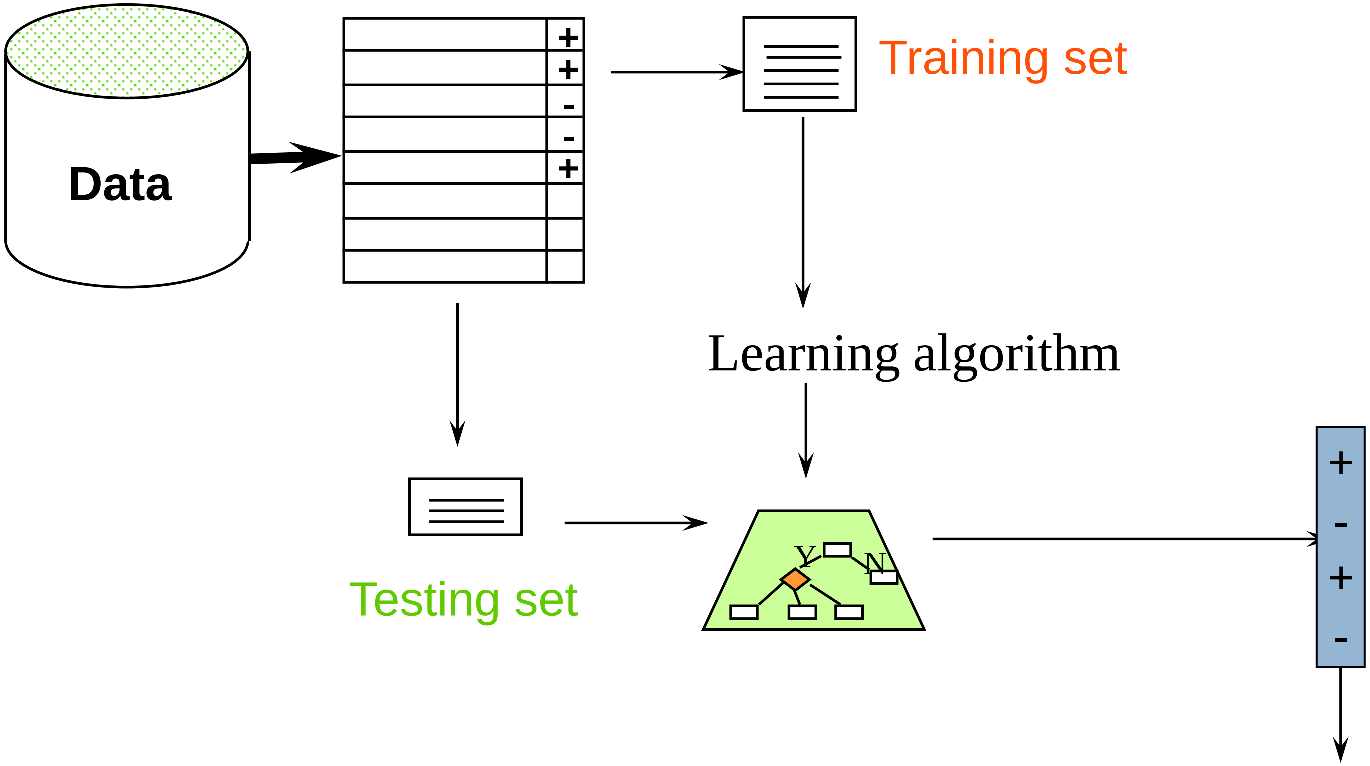
Data

Training set

Learning algorithm

Testing set

Step 3: testing the model



Results Known

Data

Training set

Learning algorithm

Testing set

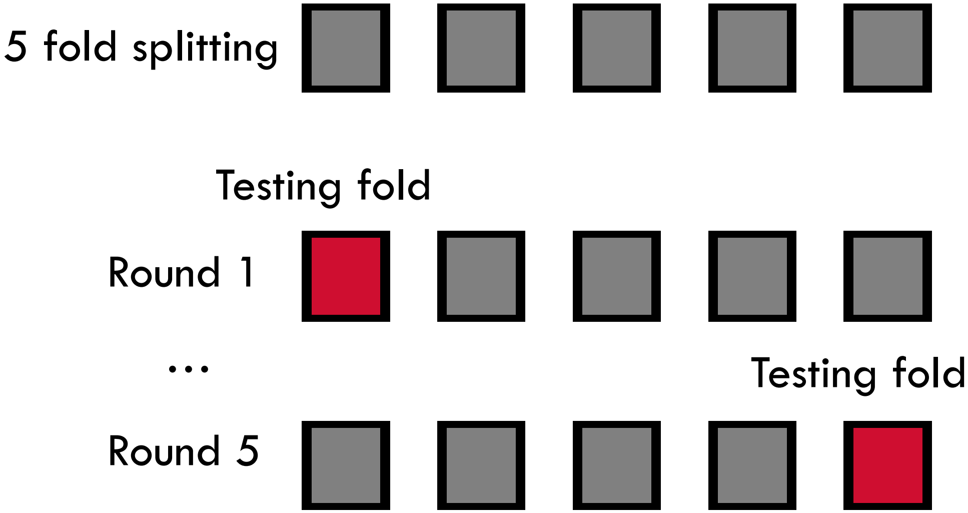
Evaluation: comparison with the oracle

Evaluation on Few Data

- When data is scarce (totally or for a single class), a single evaluation process could not be enough representative
  - The testing set could contain too few instances to produce a reliable result
- SAMPLING: The evaluation process must be repeated with different splitting

N-Fold Cross Validation

- Data is split into *n* subsets of equal size
- Each subset in turn is used for testing and the remainders *n-1* for training
- The metrics estimated in each round are averaged



5 fold splitting

Testing fold

Round 1

…

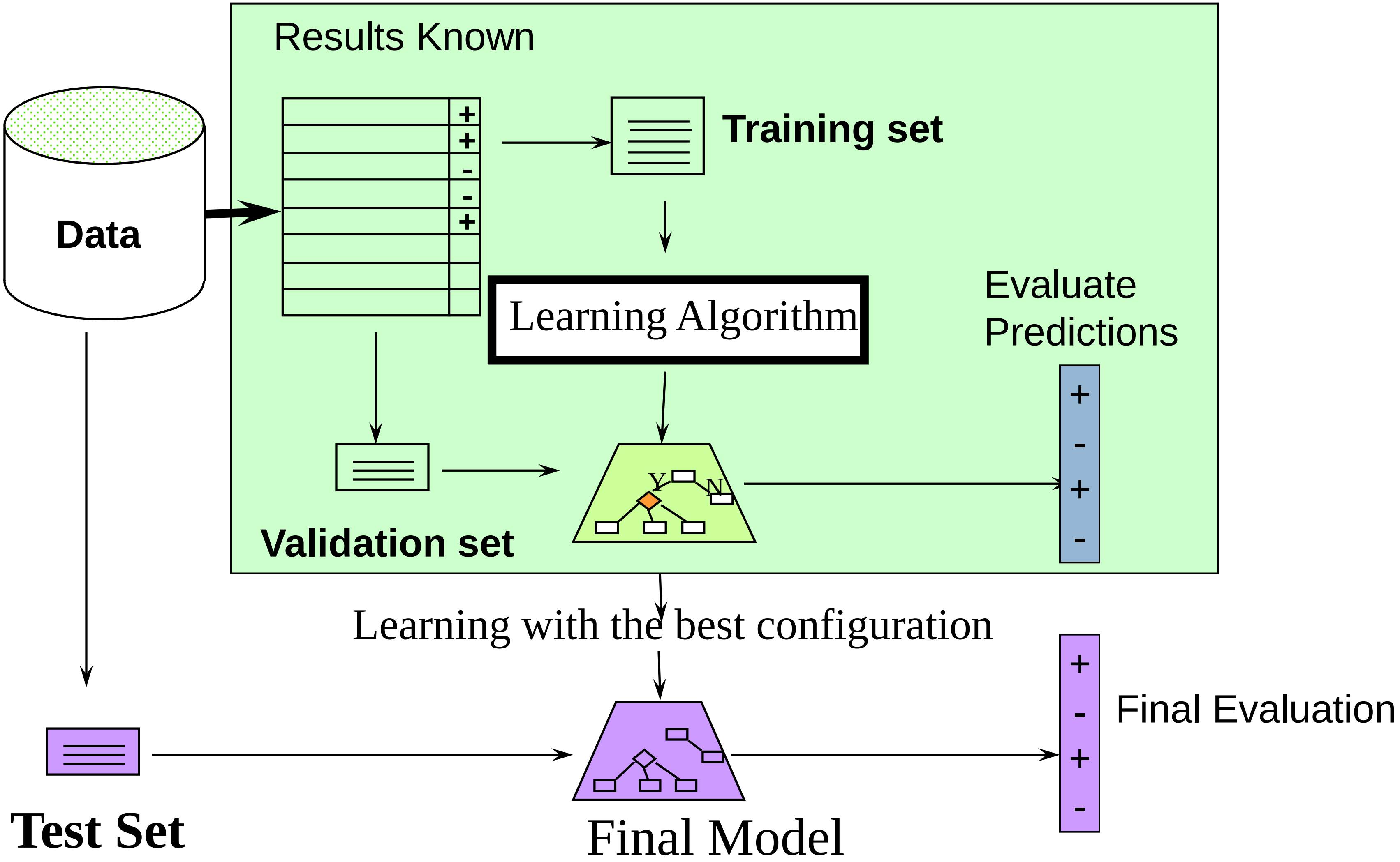
Testing fold

Round 5

Tuning a Classifier

- Most of ML algorithms depends on some parameters
  - Examples: k in KNN, w_i in Rocchio, $p(w_i \mid c_j)$ for NB
- The best configuration must be choosen after a proper tuning stage:
  - A set of configurations must be established (for instance, $k=1,2,5,10,\ldots,50$)
  - Each configuration must be evaluated on a validation (or tuning) set

Complete ML Process



Reuters text classification

- An example: the Reuters news text classification use case
  - Some well known classifiers (e.g. k-NN or SVM) are compared with a parametrized version of Rocchio
  - In the next slides, the parametrization procedure is presented and its evaluation is discussed

Feature Selection in Parametrized Rocchio

- Literature work uses a bunch of values for β and γ
- Interpretation of positive (β) vs. negative (γ) information
- ⇒ value of β > γ (e.g. 16, 4)

- IJAIT interpretation: Parametrized Rocchio [IJAIT 2002, ECIR 2003]:
- Remove one parameters (i.e. β) and let the remaining parameter to depend on the *i*-th class C^i

$$C_f^i = \max\left\{0, \frac{1}{|T_i|}\sum_{d\in T_i} d_f - \frac{\rho_i}{|\bar{T}_i|}\sum_{d\in \bar{T}_i} d_f\right\}$$

- 0 weighted features f do not affect similarity estimation
- increasing ρ causes many feature to be set to 0 ⇒ they are removed
- Different values ρ_i of the parameter are used for different classes C^i

Experiments

- Reuters Collection 21578 Apté split (Apté94)
  - 90 classes (12,902 docs)
  - A fixed splitting between training and test set
  - 9603 vs 3299 documents
- Tokens
  - about 30,000 different
- Other different versions have been used but …

  most of TC results relate to the 21578 Apté
  - [Joachims 1998], [Lam and Ho 1998], [Dumais et al. 1998], [Li Yamanishi 1999], [Weiss et al. 1999],

    [Cohen and Singer 1999]…

A Reuters document- Acquisition Category

CRA SOLD FORREST GOLD FOR 76 MLN DLRS - WHIM CREEK

SYDNEY, April 8 - <Whim Creek Consolidated NL> said the consortium it is leading will pay 76.55 mln dlrs for the acquisition of CRA Ltd's <CRAA.S> <Forrest Gold Pty Ltd> unit, reported yesterday.

CRA and Whim Creek did not disclose the price yesterday.

Whim Creek will hold 44 pct of the consortium, while <Austwhim Resources NL> will hold 27 pct and <Croesus Mining NL> 29 pct, it said in a statement.

As reported, Forrest Gold owns two mines in Western Australia producing a combined 37,000 ounces of gold a year. It also owns an undeveloped gold project.

A Reuters document- Crude-Oil Category

FTC URGES VETO OF GEORGIA GASOLINE STATION BILL

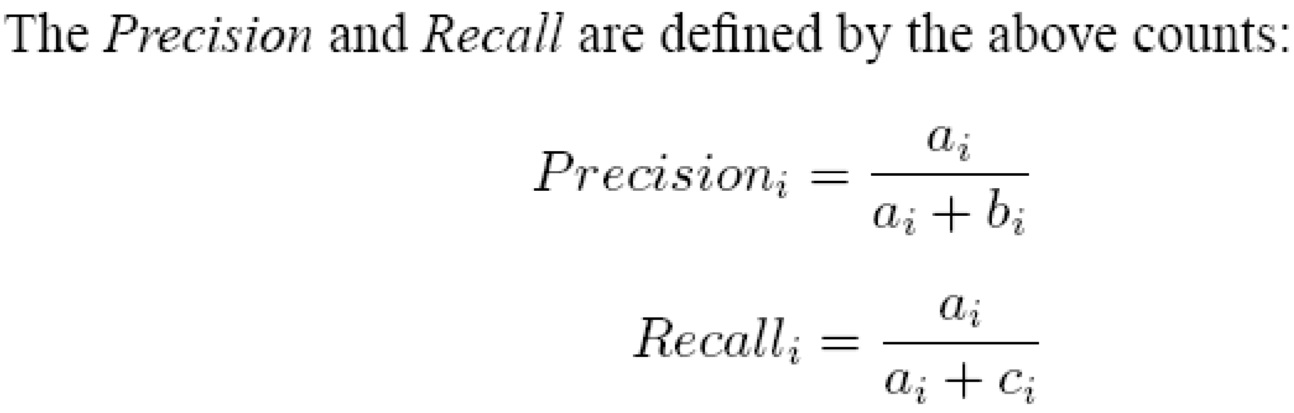
WASHINGTON, March 20 - The Federal Trade Commission said its staff has urged the governor of Georgia to veto a bill that would prohibit petroleum refiners from owning and operating retail gasoline stations.

The proposed legislation is aimed at preventing large oil refiners and marketers from using predatory or monopolistic practices against franchised dealers.

But the FTC said fears of refiner-owned stations as part of a scheme of predatory or monopolistic practices are unfounded. It called the bill anticompetitive and warned that it would force higher gasoline prices for Georgia motorists.

Precision and Recall of C_i

- a, corrects
- b, mistakes
- c, not retrieved



The *Precision* and *Recall* are defined by the above counts:

$$Precision_i = \frac{a_i}{a_i + b_i}$$

$$Recall_i = \frac{a_i}{a_i + c_i}$$

F-measure e MicroAverages

$$F_1 = \frac{2 \times Precision \times Recall}{Precision + Recall}$$

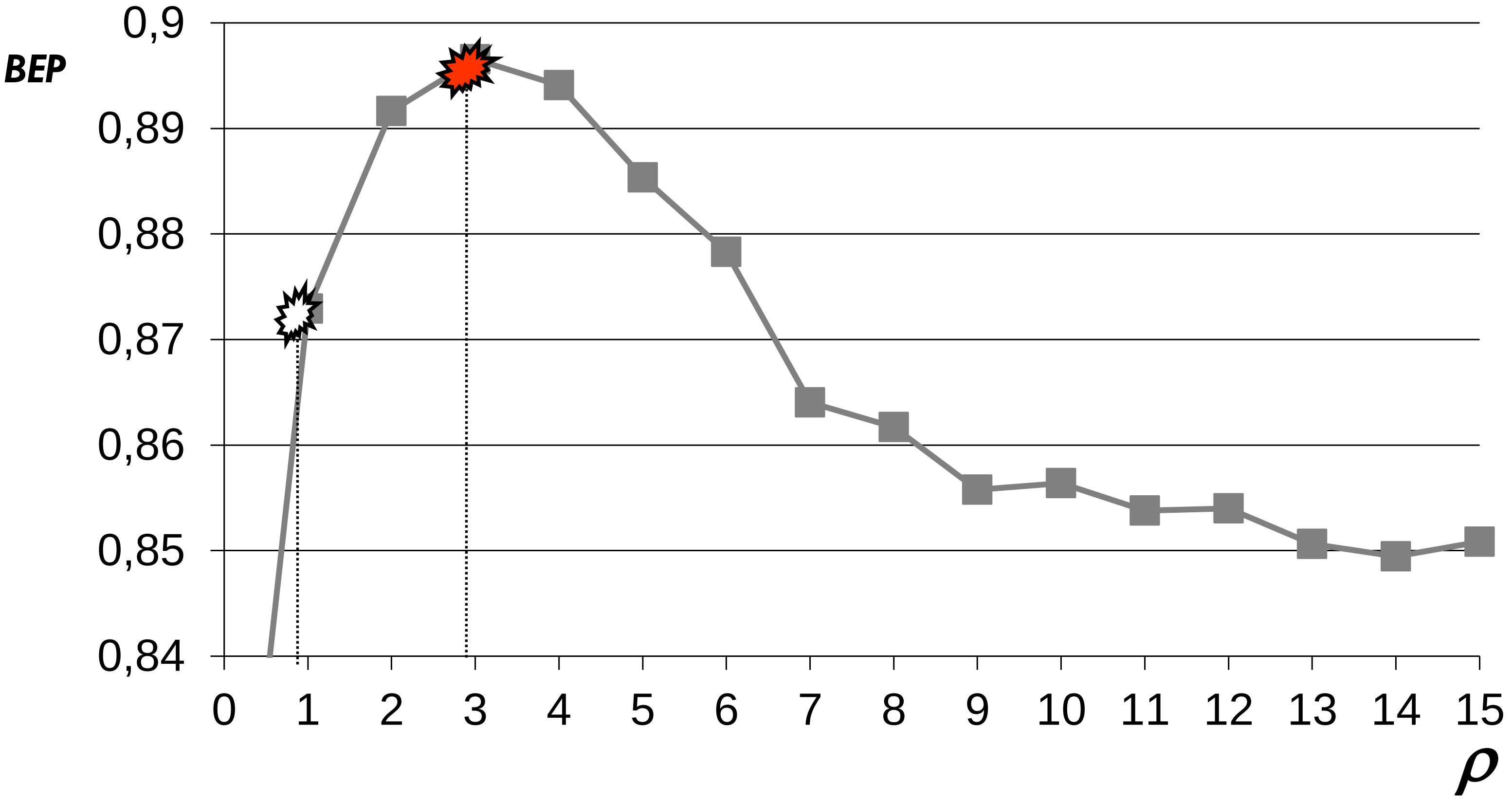
$$\mu Precision = \frac{\sum_{i=1}^{n} a_i}{\sum_{i=1}^{n} a_i + b_i}$$

$$\mu Recall = \frac{\sum_{i=1}^{n} a_i}{\sum_{i=1}^{n} a_i + c_i}$$

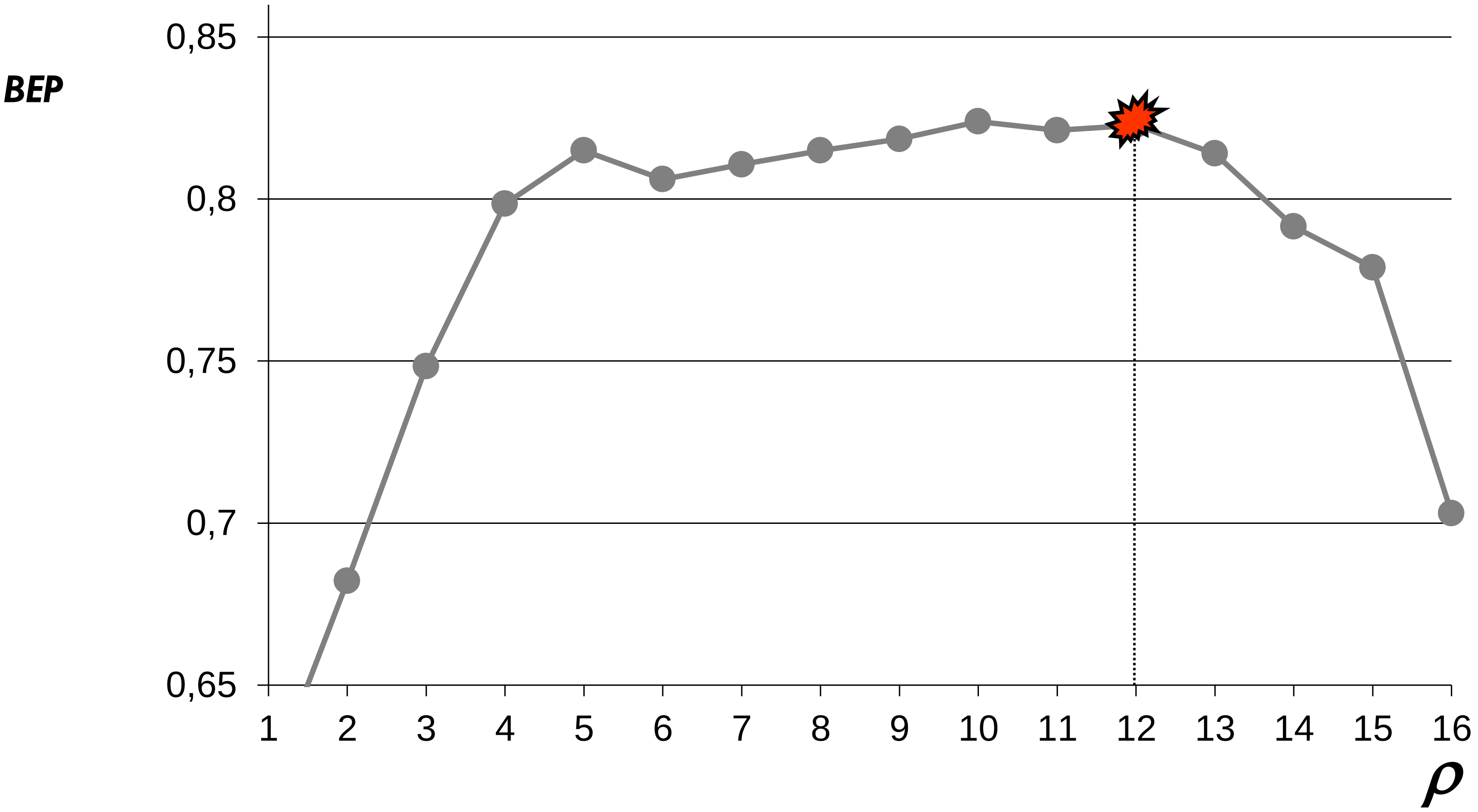
$$\mu BEP = \frac{\mu Precision + \mu Recall}{2}$$

$$\mu f_1 = \frac{2 \times \mu Precision \times \mu Recall}{\mu Precision + \mu Recall}$$

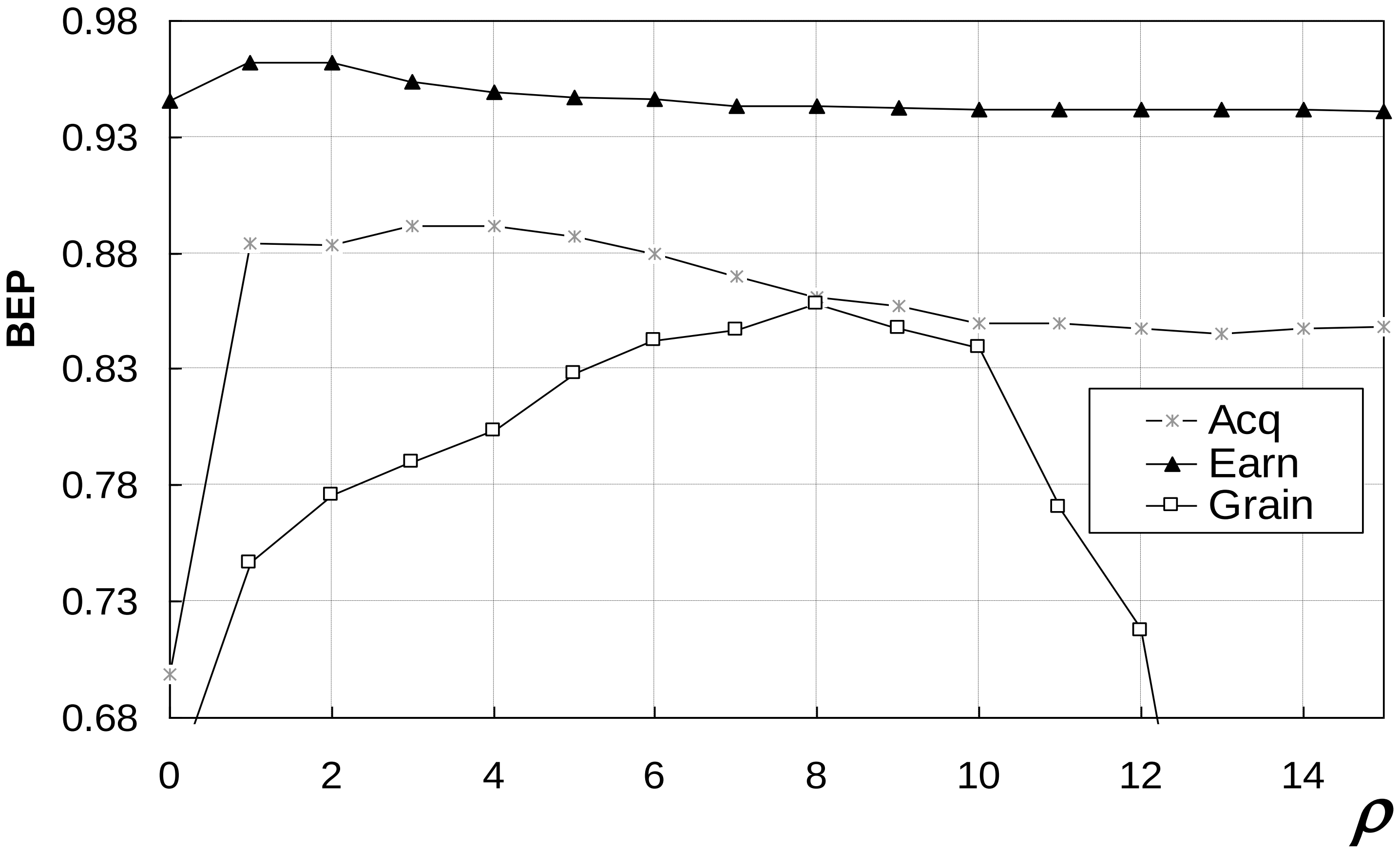
The Impact of ρ parameter on Acquisition category



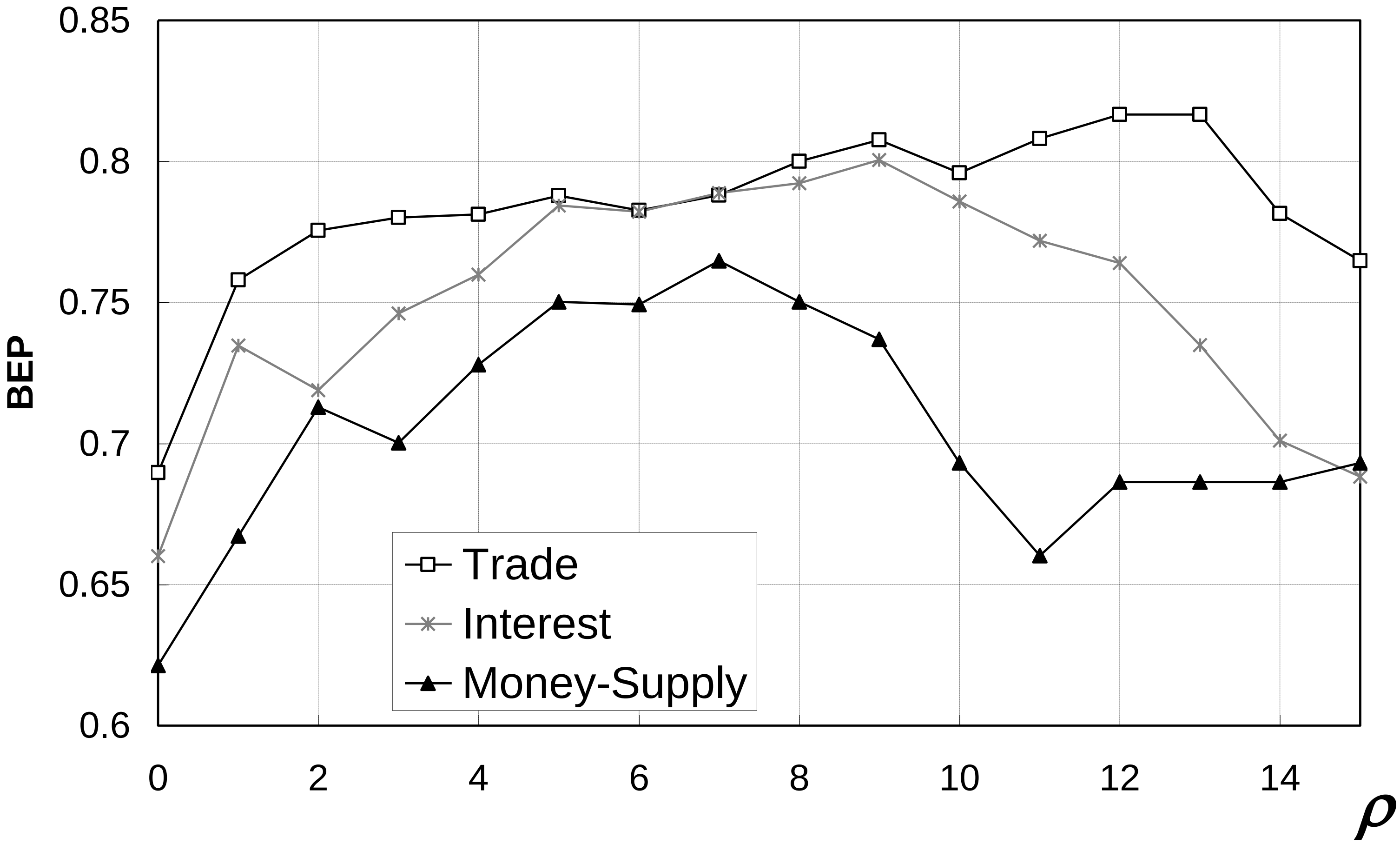
The impact of ρ parameter on Trade category



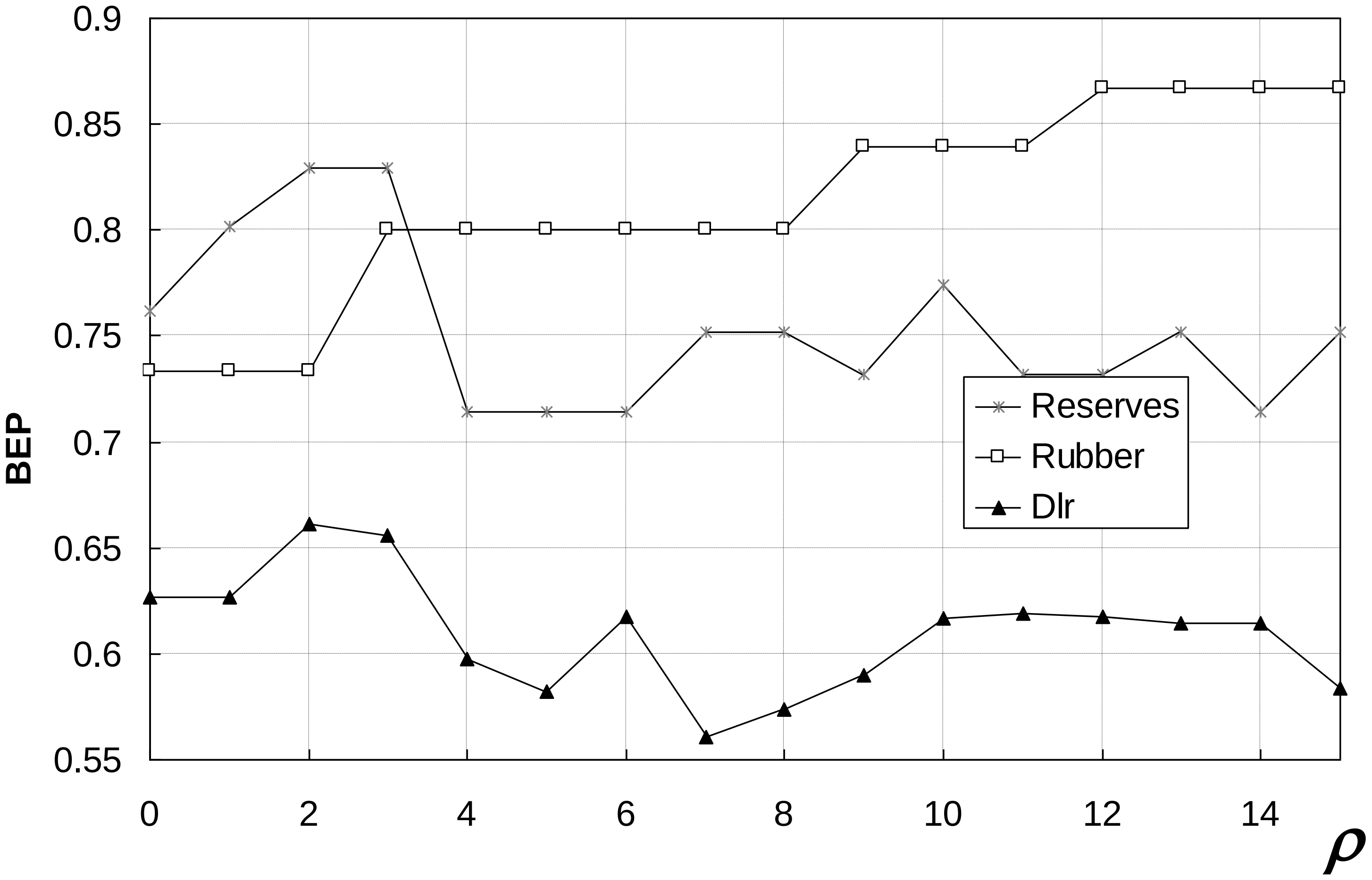
Mostly populated categories



Medium sized categories



Small size categories



Parameter Estimation Procedure

- Validation-set of about 30% of the training corpus
- for all $\rho \in [0,30]$
  - TRAIN the system on the remaining material
  - Measure the BEP on the validation-set
- Pick-up the ρ associated to the highest *BEP*
- re-TRAIN the system on the entire training-set
- TEST the system based on the obtained parameterized model
- For more reliable results:
  - 20 cross fold validation: 20 validation-sets and ρ as the average
- The Parameterized Rocchio Classifier will refer to as PRC

Comparative Analysis

- Rocchio literature parameterization
  - $\rho = 1$ ($\gamma = \beta$=1) *and* ρ = ¼ (γ = 4, β=16)
- Reuters fixed test-set
  - Other literature results
- SVM
  - To better collocate our results
- Cross Validation (20 samples)
  - More reliable results
- Cross corpora/language validation
  - Reuters, Ohsumed (English) and ANSA (Italian)

Results on Reuters fixed split

Feature Set (~30.000)	PRC	Std Rocchio ($\gamma = ¼ \beta$ or $\gamma = \beta$)	SVM
Tokens	82.83 %	72.71%-78.79%	85.34 %
Literature (stems)	-	75 % - 79.9%	84.2 %

- □ Rocchio literature results (Yang 99', Choen 98', Joachims98')
- □ SVM literature results (Joachims 98')

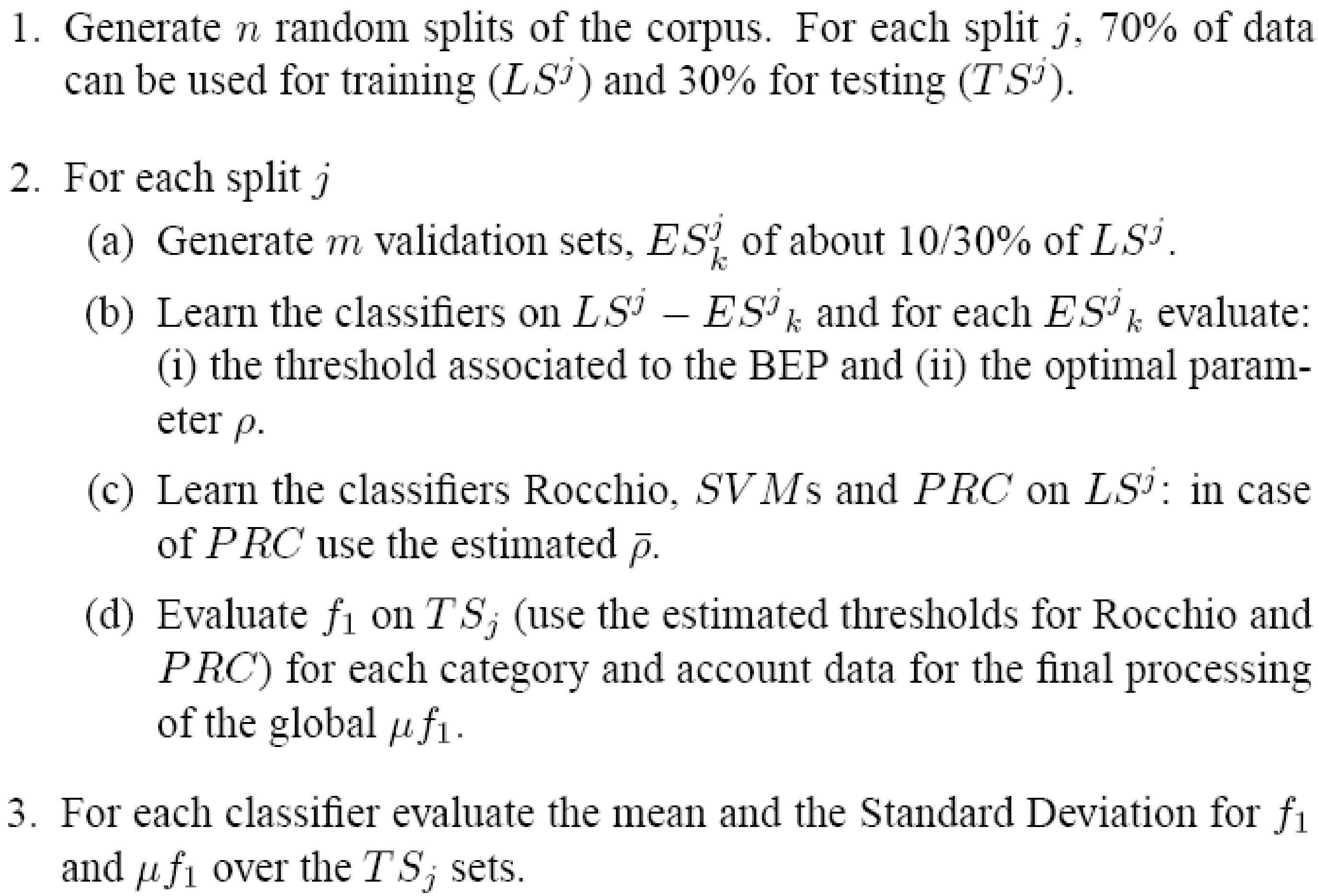
Breakeven points of widely known classifiers on the Reuters dataset

SVM	**PRC**	KNN	RIPPER	CLASSI*	Dtree
85.34%	82.83%	82.3%	82%	80.2%	79.4%

SWAP1*	CHARADE*	EXPERT	Rocchio	Naive Bayes
80.5%	78.3%	82.7%	72%-79.5%	75% - 79.9%

* Evaluation on different Reuters versions

Cross-Validation



1. Generate n random splits of the corpus. For each split j, 70% of data can be used for training (LS^j) and 30% for testing (TS^j).

2. For each split j
   (a) Generate m validation sets, ES^j_k of about 10/30% of LS^j.
   (b) Learn the classifiers on $LS^j - ES^j{}_k$ and for each $ES^j{}_k$ evaluate: (i) the threshold associated to the BEP and (ii) the optimal parameter ρ.
   (c) Learn the classifiers Rocchio, SVMs and PRC on LS^j: in case of PRC use the estimated $\bar{\rho}$.
   (d) Evaluate f_1 on TS_j (use the estimated thresholds for Rocchio and PRC) for each category and account data for the final processing of the global μf_1.

3. For each classifier evaluate the mean and the Standard Deviation for f_1 and μf_1 over the TS_j sets.

Cross-Validation on Reuters (20 samples)

	Rocchio				PRC		SVM	
	RTS		TS^{σ}		RTS	TS^{σ}	RTS	TS^{σ}
	ρ=.25	ρ=1	ρ=.25	ρ=1				
earn	95.69	95.61	92.57±0.51	93.71±0.42	95.31	94.01±0.33	98.29	97.70±0.31
acq	59.85	82.71	60.02±1.22	77.69±1.15	85.95	83.92±1.01	95.10	94.14±0.57
money-fx	53.74	57.76	67.38±2.84	71.60±2.78	62.31	77.65±2.72	75.96	84.68±2.42
grain	73.64	80.69	70.76±2.05	77.54±1.61	89.12	91.46±1.26	92.47	93.43±1.38
crude	73.58	80.45	75.91±2.54	81.56±1.97	81.54	81.18±2.20	87.09	86.77±1.65
trade	53.00	69.26	61.41±3.21	71.76±2.73	80.33	79.61±2.28	80.18	80.57±1.90
interest	51.02	58.25	59.12±3.44	64.05±3.81	70.22	69.02±3.40	71.82	75.74±2.27
ship	69.86	84.04	65.93±4.69	75.33±4.41	86.77	81.86±2.95	84.15	85.97±2.83
wheat	70.23	74.48	76.13±3.53	78.93±3.00	84.29	89.19±1.98	84.44	87.61±2.39
corn	64.81	66.12	66.04±4.80	68.21±4.82	89.91	88.32±2.39	89.53	85.73±3.79
MicroAvg. 90 cat.	72.61	78.79	73.87±0.51	78.92±0.47	82.83	83.51±0.44	85.42	87.64±0.55

Overview

- **Performance Evaluation Metrics**
  - Classifier Evaluation Metrics
  - Information Retrieval System Evaluation Metrics
- Tuning and Evaluation Methods
- Error Diagnostics

Summary

- The effectiveness of ML or IR systems can be assessed with different evaluation metrics
  - we saw just the most popular, but a lot of other metrics exist!!!
- A reliable evaluation should follow some guideline